

Miami Physics Conference 2022

Philip Mannheim

Title: Faraday's law via a variational principle, torsion and magnetic monopoles

Even though Faraday's Law is a dynamical law that describes how changing \mathbf{E} and \mathbf{B} fields influence each other, by introducing a vector potential A_{μ} according to $F_{\mu\nu} = \partial_{\mu}A_{\nu} - \partial_{\nu}A_{\mu}$ Faraday's Law is satisfied kinematically, with the relation $(-g)^{-1/2}\epsilon^{\mu\nu\sigma\tau}\nabla_{\nu}F_{\sigma\tau} = 0$ holding on every path in a variational procedure or path integral. In a space with torsion $Q_{\alpha\beta\gamma}$ the axial vector $S^{\mu} = (-g)^{1/2}\epsilon^{\mu\alpha\beta\gamma}Q_{\alpha\beta\gamma}$ serves as a chiral analog of A_{μ} , and via variation with respect to S_{μ} one can derive Faraday's Law dynamically as a stationarity condition. With S_{μ} serving as an axial potential one is able to introduce magnetic monopoles without S_{μ} needing to be singular or have a non-trivial topology.